

6-2-2014 Arun Ash. Glennfest

12:00.

Explicit computation of p -adic variations
of homology.

(distribution modules)

↑
compute.

(I) Congruence between Hecke eigenvalues.

in $H_g(\Gamma, V_\lambda)$ and $H_g(\Gamma, V_{\lambda'})$

irred. reps

with highest wt λ

mod p -power if $\lambda \equiv \lambda' \pmod{(p-1) \cdot p^\alpha}$.

today's
focus

$\rightarrow \Gamma \subset SL_3(\mathbb{Z})$

$\lambda = (a, b, c) \in \mathbb{Z}^3$.

$a \geq b \geq c$.

To interpolate the coefficients,

replace V_λ (f.d. sp.)

by D_λ (∞-dim sp.)

↑
modules of p -adic distributions

D_λ

- They are Verma modules so can be defined like for any p -adic λ .

- They are p -adic Banach spaces

- They vary p -adically analytically in λ .

- Have a comparison between

$$H_g(\Gamma, D_\lambda)^{(\leq h)} \xrightarrow{\cong} H_g(\Gamma, V_\lambda)^{(\leq h)}$$

(induced by a homomorphism $D_\lambda \rightarrow V_\lambda$).

if λ is ^a the dominant integral weight.

If $h < m(\lambda)$

↑
positive number

p -adic functional analysis

$$\frac{GL_3}{U}, \quad p \geq 5.$$

B , upper triangular.

$$\pm B = B^{opp}$$

$N \cdot T$

unipotent
diagonal.

I , Iwahori subgp. $\subseteq GL_3(\mathbb{Z}_p)$.

\Leftarrow upper triangular mod p .

$$\Gamma = T_0(M) \cap I.$$

$X =$ "big cell"

$=$ image of I in T

$B(\mathbb{Z}_p)$

$$T = N^{opp} \cdot GL_3(\mathbb{Q}_p) \setminus GL_3(\mathbb{Q}_p).$$

$$\lambda : T(\mathbb{Z}_p) \rightarrow \mathbb{C}_p^\times \quad \text{conti. char.}$$

torus
action \rightarrow

$$A_\lambda = \left\{ f : X \rightarrow \frac{\mathbb{C}_p}{\mathbb{C}_p} : f(\pm \cdot x) = \lambda(\pm) \cdot f(x) \right\}$$

and
 f is rigid analytic.

$$f \begin{pmatrix} 1 & x & y \\ 0 & 1 & z \\ c & 0 & 1 \end{pmatrix} = \sum c_{ijk} \cdot x^i \cdot y^j \cdot z^k$$

$$c_{ijk} \rightarrow 0.$$

(assuming λ is analytic)

$$D_\lambda = \text{Hom}_{\text{cts}}(A_\lambda, \mathbb{C}_p) \cong \text{Hom}_{\mathbb{Z}}(\Gamma, \mathbb{C}_p)$$

$$\cong \sum_{rst} b_{rst} \cdot \delta_{rst}^\lambda$$

We need

1) A way to compute $H_3(\Gamma, A)$
~~2~~ for any module A .

2) A way to compute Hecke operators.

Joint with David Pollack.

$h < \frac{m(\lambda)}{\text{critical slope}}$.

3) A way to lift from $H_3(\Gamma, V_{x_0}) \leq h$.

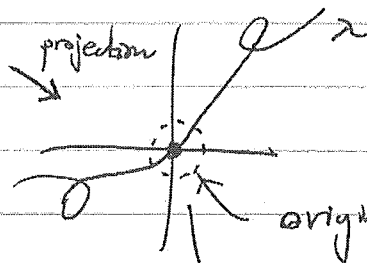
to $H_3(\Gamma, D_{x_0}) \leq h$.

4) Deform from $H_3(\Gamma, D_{x_0})$ to

to nearby $H_3(\Gamma, D_x) \stackrel{\exists}{\rightarrow} f, \text{ eigen}$

eigenvalues

projection



origin = classical sit.

can get the tangent vector
(hopefully @ eqns.)

idea.

$$\frac{F|U^n}{\alpha^n} \rightarrow \text{eigenclass.}$$

$$Au = \alpha f$$