Math 124, Practice Exam Questions for Exam #1, February 23, 2001

- 1. Find the following:
 - (a)

$$\int \sin^{100}(x) \cos(x) \, dx$$

(b)

$$\int \frac{3x^2 - 16x + 5}{\sqrt{x^3 - 8x^2 + 5x + 3}} \, dx$$

(c)

$$\int (x-\frac{3}{2})\sin(x^2-3x)\,dx$$

(d)

$$\int x \ln x^3 \, dx$$

(e)

 $\int e^{\sqrt{x}} dx$

(f)

$$\int_0^{\frac{\pi}{4}} \tan^5 x \sec^2 x \, dx$$

(g)

$$\int_2^4 f'(x)\sin(f(x))dx$$

if f is a continuous function on the interval [0, 20] such that f(0) = 3, f(2) = 1, f(4) = 7, and f(20) = 5.

(h)

$$\int_{1}^{3} (2x-8)e^{-x} \, dx$$

(i)

$$\int_{-\infty}^{3} \frac{1}{1+x^2} \, dx$$

(j) \bar{f} , the average value of $f(x) = x^2$ over the interval [3,8].

2. Consider the region R in the xy-plane where $x \ge 0$ bounded by the graphs $y = x^3$ and $y = x^5$.

- (a) Calculate the area of R.
- (b) Calculate the centroid of R.
- (c) Consider the solid S whose base is R and whose cross-sections perpendicular to the x-axis are equilateral triangles. Find the volume V of S.

- 3. Find the arc length of the part of the curve $y = 2x^{\frac{3}{2}}$ between the points (1,2) and (4,16).
- 4. Consider the region Q in the xy-plane bounded by the graphs y = x and $y = (x 2)^2$. Find the volume of the solid obtained by revolving Q about the x-axis.
- 5. Consider the differential equation

$$\frac{dy}{dx} + 2y = e^x.$$

(a) Verify that

$$y = Ce^{-2x} + \frac{1}{3}e^x$$

is a solution for any constant C.

(b) Find the solution which satisfies y(0) = 8.