

Math 124, Practice Exam Questions for Exam #1, February 23, 2000

1. Find the following:

(a)

$$\int \sin^{100}(x) \cos(x) dx$$

(b)

$$\int \frac{3x^2 - 16x + 5}{\sqrt{x^3 - 8x^2 + 5x + 3}} dx$$

(c)

$$\int \left(x - \frac{3}{2}\right) \sin(x^2 - 3x) dx$$

(d)

$$\int x \ln x^3 dx$$

(e)

$$\int_0^{\frac{\pi}{4}} \tan^5 x \sec^2 x dx$$

(f)

$$\int_2^4 f'(x) \sin(f(x)) dx$$

if  $f$  is a continuous function on the interval  $[0, 20]$  such that  $f(0) = 3$ ,  $f(2) = 1$ ,  $f(4) = 7$ , and  $f(20) = 5$ .

(g)

$$\int_1^3 (2x - 8)e^{-x} dx$$

(h)  $\bar{f}$ , the average value of  $f(x) = x^2$  over the interval  $[3, 8]$ .

2. Consider the region  $R$  in the  $xy$ -plane where  $x \geq 0$  bounded by the graphs  $y = x^3$  and  $y = x^5$ .

(a) Calculate the area of  $R$ .

(b) Calculate the centroid of  $R$ .

3. Find the arc length of the part of the curve  $y = 2x^{\frac{3}{2}}$  between the points  $(1, 2)$  and  $(4, 16)$ .

4. Consider the region  $Q$  in the  $xy$ -plane bounded by the graphs  $y = x$  and  $y = (x - 2)^2$ . Find the volume of the solid obtained by revolving  $Q$  about the  $x$ -axis.