## Math 563A1, Homework 2 Due October 4, 2006 Prof. Takashi Kimura

- 1. (10 points) Pressley Problem 4.16.
- 2. (10 points) Show that the hyperboloid of one sheet S is a smooth surface where S consists of points (x, y, z) such that

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1.$$

- 3. (10 points) Pressley Problem 4.19.
- 4. (20 points) Consider a circle of radius r in the xz-plane whose center lies on the x-axis a distance R from the origin. Rotate this circle about the z-axis to obtain a torus S.
  - (a) Show that S has an atlas consisting of surface patches of the form

 $\sigma(u, v) := ((R + r\cos u)\cos v, (R + r\cos u)\sin v, r\sin u)$ 

where (u, v) belong to suitable open subsets of  $\mathbb{R}^2$ .

- (b) Calculate the standard unit normal  $N_{\sigma}$ .
- (c) Find the equation for  $T_pS$ , the tangent plane to S at the point p where  $p := (R/\sqrt{2}, R/\sqrt{2}, r).$
- (d) Calculate the first fundamental form of  $\sigma$ .