- 1. Find the following:
 - (a)

$$\lim_{y \to \infty} \left(1 + \frac{2}{y} \right)^y$$

(b)

$$\lim_{x \to 0} \frac{\cos\left(\sqrt{5}\,x\right) \,-\, 1}{x^2}$$

(c)

$$\lim_{x \to 0} \left(\frac{1}{x} - \frac{1}{\sin x} \right)$$

(d) The horizontal and vertical asymptotes of

$$y = \frac{4 - 3x}{\sqrt{16x^2 + 1}}$$

- 2. A man 6 feet tall is walking away from a light pole which is 30 feet high. If the tip of his shadow is moving at a rate equal to the distance between him and the light pole (in feet) then how fast is the man walking when he is 24 feet from the pole?
- 3. A spherical snowball is melting at a rate equal to its surface area. How fast is its radius shrinking when its volume is equal to its surface area?
- 4. Two nonnegative numbers are such that the sum of the first number and 3 times the second number equals 10. Find these numbers if the sum of their squares is as small as possible.
- 5. If 12cm³ of material is available to make a box with a square base and an open top, find the dimensions of the box which maximizes the the volume of the box. What is this maximum volume? Justify your answer.
- 6. Calculate the following:
 - (a) Find the most general antiderivative F(x) of $f(x) = \frac{x^3 + 4\sqrt{x}}{x}$.
 - (b) Find the antiderivative F(x) from above satisfying F(1) = 0.
- 7. Consider the function

$$f(x) = 3x^4 - 4x^3 + 20000$$

- (a) On what interval(s) is f increasing?
- (b) On what interval(s) is f concave down?

- (c) Find the inflection point(s) of f.
- (d) Find the critical points of f.
- (e) Find the local maximum (maxima) of f.
- (f) Find the global minimum of f on the interval [-1, 2].
- 8. Repeat the previous problem for

$$f(x) = |x^2 - 5|$$

- 9. Suppose the graph on the following page is of y = f(x)
 - (a) Find the critical numbers of f.
 - (b) On what interval(s) is f increasing?
 - (c) On what interval(s) is f concave down?
 - (d) Find the values of x on the interval $(-\infty, \infty)$ where f has a local minimum.
 - (e) Find the values of x on the interval [0, 4] where f has a global minimum.
 - (f) Find the x values of all inflection points of f.
- 10. Suppose the graph on the following page is of y = f'(x) (**NOT** f(x)).
 - (a) Find the critical numbers of f.
 - (b) On what interval(s) is f increasing?
 - (c) On what interval(s) is f concave down?
 - (d) Find the values of x on the interval $(-\infty, \infty)$ where f has a local minimum.
 - (e) Find the values of x on the interval [0, 4] where f has a global minimum.
 - (f) Find the x values of all inflection points of f.