Summer Term I Kostadinov MA124 Calculus II Boston University

## Quiz No.0

student:

**Problem 1:** Give an example of an increasing function with domain the set of all real numbers  $\mathbb{R}$  and range the set of all positive real numbers  $\mathbb{R}^+$ 

**Problem 2:** Give an example of a function of each of the following types: power function exponential function trigonometric function -

**Problem 3:** Draw, by hand, a rough sketch of the graph of the following functions:



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**Problem 4:** Compute  $(a + b)(a^2 - ab + b^2)$ , where a and b are the roots of the equation  $x^2 + 3x - 4 = 0$ 

**Problem 5:** Find the limits:

a) 
$$\lim_{x \to -3} \frac{x^2 - 9}{x^2 + 2x - 3}$$
  
b) 
$$\lim_{x \to 1} e^{x^3 - x}$$
  
c) 
$$\lim_{x \to \infty} \frac{\sin(x)}{x}$$

**Problem 6:** What does the 'squeeze' theorem says? (Provide the statement, or give a rough idea, or give an example of applying the theorem, or sketch by hand a picture illustrating the theorem)

**Problem 7:** Using  $\Sigma$  notation, rewrite the sum  $3^2 + 4^2 + 5^2 + \cdots + 100^2 =$ Expand the shorthand notation  $\sum_{k=1}^{n} 2^k =$ 

Problem 8: Write the derivatives of the following functions

a) 
$$y = e^x$$
 c)  $y = x^n$ 

b) 
$$y = \ln(x)$$
 d)  $y = \sin(x)$ 

**Problem 9:** Compute y' if  $y = x^2(e^x + \ln(x))$ .

**Problem 10:** If in a given interval the derivative of a function is positive, then the function is *increasing decreasing* in the interval. (cross out the WRONG word)