

## Quiz No.19

student:

**Problem 1:** The sum of the series  $\sum_{n=0}^{\infty} \frac{x^n}{n!}$  is a well known function. Which one?

**Problem 2:** Write the expansion of  $\frac{1}{1-x}$  as a power series. What is the interval of convergence?

**Problem 3:** Knowing that  $\sin(x) = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!}$  for all  $x$ , write down the expansion of  $\cos(x)$  as power series.

**Problem 4:** Using your answer for problem 3 and differentiation, give the expansion as a power series of the function  $\frac{1}{(1-x)^2}$ .

**Problem 5:** Using your answer for problem 3, give the expansion as a power series of the function  $\ln(1-x)$ . What is the radius of convergence?

**Problem 6:** Maclaurin Series.

If  $f$  has a power series expansion

$f(x) = \sum_{n=0}^{\infty} c_n x^n$  for some interval  $|x - 0| < R$ , then the coefficients are given by  $c_n = \dots$

**Problem 7:** Taylor Series.

If  $f$  has a power series expansion around  $a$

$f(x) = \sum_{n=0}^{\infty} c_n (x - a)^n$  for some interval  $|x - a| < R$ , then the coefficients are given by  $c_n = \dots$

**Problem 8:** Suppose  $e^{2x}$  has a power series expansion. Find the first four term of the series.

**Problem 9:** Find the expansion of the function  $x^2 + x + 1$  around 2.

**Problem 10:** Find the radius of convergence and the interval of convergence of the series  $\sum_{n=0}^{\infty} \frac{(x+2)^n}{n!}$