Boston University Summer I 2010 Number Theory Kalin Kostadinov

## **Homework No.4**

student: due 05/27/2010

**Problem A:** Use the Chinese Remainder Theorem to show that the following system of linear congruences has a unique solution modulo 600, then find it.

 $\begin{array}{c|ccccc}
P & C & N \\
-/6 & -/2 & -/2
\end{array}$ 

 $5x \equiv 4 \pmod{24}$  $11x \equiv 52 \pmod{75}$  $17x \equiv 44 \pmod{100}$ 

**Problem B:** Let a, b be integers, and m, n positive numbers, such that n|m. Prove that if  $a \equiv b \pmod{m}$ , then  $a \equiv b \pmod{n}$  as well. Boston University Summer I 2010 Number Theory Kalin Kostadinov

Problem C: Using the list of axioms from the workshop, prove that the<br/>product  $1' \times 1'$  equals 1. $P \ C \ -/2 \ -/2$ 

**Problem D:** Complete the online test 'The Logic of Proofs' available on the course Blackboard site.