Boston University Summer I 2010 Number Theory Kalin Kostadinov

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Homework No.5

student: due 06/01/2010

Problem A: Use the projection from a rational point method to find a parametrization of all the integer solutions of the equation $x^2 + y^2 = 5z^2$. Include only the crucial steps.

Problem B: Find all integer x, y such that 17x - 11y = 75.

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Problem C: Compute $gcd(2^9 - 1, 2^{15} - 1)$. Do same for $gcd(2^{10} - 1, 2^{15} - 1)$ and $gcd(2^{11} - 1, 2^{15} - 1)$? Make a conjecture what would be $gcd(2^m - 1, 2^{15} - 1)$ for an arbitrary $m \in \mathbb{N}$.

Problem D: Find a blog-post with content related to the topics we have discussed so far in class, and summarize the post and what you think is intresting about it. $\frac{P}{-/6} \begin{bmatrix} C & N \\ -/2 & -/2 \end{bmatrix}$