

Lecture on July 2nd, 2018  
Conditional Probability and Conditional Expectations I

**1 Conditional Probability (Discrete Case) - See Chap 2.1**

- Definitions of conditional probabilities, conditional mass function.
- Conditional mass function is a probability mass function!
- Example: If  $X \sim B(N, p)$ ,  $N \sim B(M, q)$ , then  $X \sim B(M, pq)$ .

**2 Conditional Expectation (Discrete Case) - See Chap 2.1**

- Definitions and important properties of conditional expectations.
- $\mathbb{E}[g(X)|Y = y]$  is a function of  $y$ , and  $\mathbb{E}[g(X)|Y]$  is a random variable.

**3 Random Sums - See Chap 2.3**

- Definition of random sum.
- Definition and properties of conditional distribution function and density function.