

Lecture on July 3rd, 2018  
Conditional Probability and Conditional Expectations II

**1 Random Sums - See Chap 2.3**

- Definition of random sum.
- Definition and properties of conditional distribution function and density function.
- Moments (mean and variance) of random sum.
- Distribution of random sum.
- Example:  $\xi_i \sim Exp(\lambda)$ ,  $N \sim Geo(\beta)$ , then random sum  $X \sim Exp(\lambda\beta)$ .

**2 Conditional Probability and Expectations (Continuous Case) - See Chap 2.4**

- Definitions and properties of conditional probability density function, conditional distribution function, conditional expectation.
- Example: If  $X, Y \sim f_{X,Y}(x, y) = \frac{1}{y} \exp^{-x/y-y}$  for  $x, y > 0$ , then  $f_{X|Y}(x|y) = \frac{1}{y} \exp^{-x/y}$ , for  $x, y > 0$ .