## Lecture on July 26th, 2018 Continuous Time Markov Process

## 1 Spatial Poisson Process (See Chap 5.5)

- $For B \subset A$ ,  $\mathbb{P}(N(B) = 1|N(A) = 1) = \frac{|B|}{|A|}$ .
- For a partition of  $A, A_1, A_2, \dots, A_m$ , Conditioned on N(A) = n, the n points distributed in  $A_1, A_2, \dots, A_m$  follows multinomial distribution.

## 2 Pure Birth Process (See Chap 6.1)

- Definition of Poisson process in terms of continuous time Markov process.
- Definition of pure birth process in terms of continuous time Markov process.
- The differential equations  $P_n(t) = \mathbb{P}(X(t) = n | X(0) = 0)$  satisfies.
- Sojourn time and birth time for pure birth process.
- Example: Yule process.