

Lecture on July 23th, 2019  
Poisson Process and Law of Rare Events

## 1 Poisson Process (See 5.1)

- Review for Poisson distribution.
- Definition of homogenous and non-homogenous Poisson process.
- Method to transform a non-homogenous Poisson process to a unit homogenous Poisson process.

## 2 Law of Rare Events (See 5.2)

- Law of rare events is saying that the number of rare events happening is following a Poisson distribution.
- Example: a sum of  $N$  i.i.d. Bernoulli( $p$ ) r.v. goes to Poisson( $\mu$ ), when taking  $N \rightarrow \infty, p \rightarrow 0$  in such a way that  $Np = \mu$  fixed.
- Example of stochastic modeling, use Poisson distribution to model the number of accidents.
- Theorem on Poisson Approximation Error.