

Lecture on July 24th, 2019  
Alternative Way to define Poisson Process

**1 Alternative Way to Define a Poisson Process (See 5.2)**

- 4 postulates to define  $N((a, b])$  and a theorem to claim that  $N((0, t])$  defined in this way is a poisson process as defined in previous lecture.
- When parameter  $t$  refers to "time", usually it's called "Poisson Process". When  $t$  refers to "space", usually it's called "Poisson Point Process".

**2 Distributions Associated with Poisson Process (See Chap 5.3)**

- Waiting time  $W_n \sim \text{Gamma}(n, \lambda)$
- Sojourn time  $S_n$ 's are independent and follows  $\text{Exp}(\lambda)$ .