

BOSTON UNIVERSITY
MA 226 SECTION A

Spring Semester

Differential Equations

2017

STANDARD LAPLACE TRANSFORMS

| Function | Laplace transform |
|-------------------------|--|
| $f(t)$ | $\mathcal{L}\{f\} = F(s) = \int_0^\infty f(t)e^{-st} dt$ |
| e^{at} | $\frac{1}{s-a} \quad s > a$ |
| 1 | $\frac{1}{s} \quad s > 0$ |
| $\cos(\omega t)$ | $\frac{s}{s^2 + \omega^2} \quad s > 0$ |
| $\sin(\omega t)$ | $\frac{\omega}{s^2 + \omega^2} \quad s > 0$ |
| $t^n, n \in \mathbb{N}$ | $\frac{n!}{s^{n+1}} \quad s > 0$ |
| $H(t - a)$ | $\frac{e^{-as}}{s} \quad s > 0, a \geq 0$ |
| $\delta(t - a)$ | $e^{-as} \quad s > 0, a > 0$ |

PROPERTIES OF LAPLACE TRANSFORMS

| Function | Laplace transform |
|--|---|
| $\alpha f(t) + \beta g(t)$ | $\alpha \mathcal{L}\{f\} + \beta \mathcal{L}\{g\}$ |
| $\frac{df}{dt}$ | $s \mathcal{L}\{f\} - f(0)$ |
| $\frac{d^2 f}{dt^2}$ | $s^2 \mathcal{L}\{f\} - s f(0) - \frac{df}{dt} \Big _{t=0}$ |
| $H(t - a)f(t - a)$ | $e^{-as} \mathcal{L}\{f\}$ |
| $e^{at}f(t)$ | $F(s - a), F(s) := \mathcal{L}\{f\}$ |
| $f(t) * g(t) := \int_0^t f(t - u) g(u) du$ | $\mathcal{L}\{f\} \times \mathcal{L}\{g\}$ |