MA 294 - Turn in #1

(1) Under congruence mod m = 13, determine those $b \in U(13)$ such that (as sets)

$$\{1, 2, \dots, 12\} = \{b^1, b^2, b^3, \dots, b^{12}\}\$$

where the order of the elements on the right hand side is not necessarily the same as that on the left.

[10 points]

(2) For $i = \sqrt{-1}$, the imaginary unit, let $C = \{1, -1, i, -i\}$. Show that *C* is a group under multiplication, and compute its group table. You may assume the operation is associative.

[10 points]