BOSTON UNIVERSITY GEOMETRY SEMINAR

Yangians and quantum loop algebras

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Wednesday, Oct. 20, 3-4 pm in PSY B53 Tea 2:45-3 in MCS 153

Abstract:

For a semisimple Lie algebra \mathfrak{g} , the quantum loop algebra $U_{\hbar}L\mathfrak{g}$ and the Yangian $Y_{\hbar}\mathfrak{g}$ are certain deformations of the loop algebra $\mathfrak{g}[z, z^{-1}]$ and the current algebra $\mathfrak{g}[u]$ respectively. These two algebras are very closely related, and are believed to have the "same" representation theory. To mention a few known results relating the quantum loop algebras and the Yangians, we have the following: (a) the finite-dimensional irreducible representations of both these algebras are parametrized by certain rank(\mathfrak{g})-tuple of polynomials, called Drinfeld polynomials (b) both these algebras have geometric realizations on the same Steinberg-type variety, and (c) the Yangian can be obtained by a certain degeneration of the quantum loop algebra. Despite these results, no natural relationship between the two algebras is known. In this talk, I will explain how to construct a functor between the finite-dimensional representation categories of these two algebras. This talk is based on a joint work with Valerio Toledano Laredo.