

We consider an extension of the non-compact Calabi-Yau theorem of S. Bando, R. Kobayashi, G. Tian, and S. T. Yau. A similar construction of non-compact complete Ricci-flat metrics on quasi-projective varieties  $Y = X \setminus D$  with  $\alpha[D] = c_1(X)$ ,  $\alpha > 1$  is given, where  $D$  is a smooth divisor which in this case possibly does not admit a Kaehler-Einstein metric. This construction produces examples of Ricci-flat Kähler metrics on manifolds  $Y = X \setminus D$  where  $D$  is toric. The proof makes use of a result of A. Futaki, H. Ono, and G. Wang that the link  $S$  in the normal bundle of  $D$ , this case a toric Sasaki manifold, admits a Sasaki-Einstein metric.